1	Integrals of life: tracking ecosystem spatial
2	heterogeneity from space through the area under
3	the curve of the parametric Rao's Q index
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Abstract

Spatio-ecological heterogeneity is strongly linked to many ecological 47 processes and functions such as plant species diversity patterns and change, 48 metapopulation dynamics, and gene flow. Remote sensing is particularly 49 useful for measuring spatial heterogeneity of ecosystems over wide regions 50 with repeated measurements in space and time. Besides, developing free 51 and open source algorithms for ecological modelling from space is vital to 52 allow to prove workflows of analysis reproducible. From this point of view, 53 NASA developed programs like the Surface Biology and Geology (SBG) 54 to support the development of algorithms for exploiting spaceborne re-55 motely sensed data to provide a relatively fast but accurate estimate of 56 ecological properties in vast areas over time. Most of the indices to mea-57 sure heterogeneity from space are point descriptors : they catch only part 58 of the whole heterogeneity spectrum. Under the SBG umbrella, in this 59 paper we provide a new R function part of the rasterdiv R package which 60 allows to calculate spatio-ecological heterogeneity and its variation over 61 time by considering all its possible facets. The new function was tested on 62 two different case studies, on multi- and hyperspectral images, proving to 63 be an effective tool to measure heterogeneity and detect its changes over time. 65

*Keywords*— biodiversity, ecological informatics, modelling, remote sensing, satel lite imagery

## 68 1 Introduction

The concept of spatiotemporal heterogeneity is crucial in ecological modelling to link spatial patterns to the generating processes and to the functional networking among organisms (Borcard et al., 1992). In ecological research, the search for new methods underlying spatiotemporal patterns in ecosystem heterogeneity has been a recurring theme (Rocchini and Ricotta, 2007; Atluri et al., 2018). Spatio-ecological hetero-

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geneity, in this paper considered as the degree of non-uniformity in vegetation, land 74 cover, and physical factors (soil, topography, microclimate and topoclimate; (Stein et 75 al., 2014), has been proven to be strongly linked to many ecological processes and 76 functions such as plant species diversity patterns and change (Rocchini et al., 2018), 77 metapopulation dynamics (Fahrig, 2007), and gene flow (Lozier et al., 2013). Indeed, 78 79 an increase of spatial heterogeneity means an increase in the availability of ecological niches, provision of refuges at relatively short distances and opportunities for spatial 80 isolation and local adaptation (Stein et al., 2014). As a consequence, species coexis-81 tence, persistence and diversification are generally in strict relation with the degree of 82 environmental heterogeneity available within the landscape (Stein et al., 2014; Tews 83 et al., 2004). The development of new methods for measuring spatio-ecological het-84 erogeneity is also fundamental to make estimations of its change in time in order to 85 improve conservation planning (Skidmore et al., 2021). 86

In this context, NASA developed programs like the Global Ecosystem Dynamics 87 Investigation (GEDI, https://gedi.umd.edu/) or the Surface Biology and Geology 88 (SBG) mission (https://science.nasa.gov/earth-science/decadal-sbg) exploit-89 ing spaceborne remotely sensed data to provide a relatively fast but accurate estimate 90 of spatio-ecological heterogeneity in vast areas over time. In fact, spectral heterogene-91 ity of an optical image - associated with the reflectance values of the pixels - can be 92 a proxy of the spatio-ecological heterogeneity (Rocchini, 2007). Hence, the variation 93 of spatio-ecological heterogeneity in space and time (e.g., phenological cycles) can be 94 effectively inferred using remote sensing (Schneider et al., 2017). 95

Therefore, the measure of ecosystem heterogeneity over time from satellite through 96 Free and Open Source Software and algorithms allows robust, reproducible and stan-97 dardized estimates of ecosystem patterns and processes (Rocchini and Neteler, 2012). 98 Also, its use brings many advantages: availability, transparency and shareability. In 99 this context, the R platform is one of the most used statistical and computational 100 environment in ecology, partially thanks to the continuous development of relevant 101 packages. In particular, the rasterdiv package (Marcantonio et al., 2021; Rocchini 102 et al., 2021; Thouverai et al., 2021) allows to calculate a plethora of different indices 103

<sup>104</sup> to measure spatio-ecological heterogeneity from space.

Most of the algorithms have been related to Information Theory relying on abundance-105 based metrics, starting from Shannon's index (Shannon, 1949) (see section 2). How-106 ever, some information about the spectral distance among pixel reflectance values 107 might be lost if not considered in the calculation (Rocchini et al., 2017). Currently, 108 the candidate for solving the problem is Rao's Quadratic Entropy index (hereafter 109 Rao's Q) (Rao, 1982): this index, besides the relative abundance of pixel values in 110 a given moving window or polygonal area, incorporates also their spectral distances 111 (section 2). Both Shannon and Rao's Q indices are point descriptors of heterogene-112 ity, namely they can only show part of the whole heterogeneity spectrum. Recently 113 Rocchini et al. (2021) proposed an implementation of the Rao's Q index by param-114 eterizing the original formula, and allowing the whole continuum of heterogeneity to 115 be measured thanks to Rao's Q continuous profiles (see section 2). 116

This paper aims to show how to make proper use of the Rao's continuum heterogeneity variation profile by proposing a new R function – integrated into the **rasterdiv** R package (Marcantonio et al., 2021) - which calculates AUC, the area under the curve formed by applying the parametric Rao's Q index (see section 2). Two case studies on multi- and hyperspectral satellite images are also provided in order to verify if the new metric proposed could be an effective tool for the study of spatio-ecological heterogeneity.

## <sup>124</sup> 2 The algorithm

#### 125 2.1 The theory

Algorithms that aim to measure environmental heterogeneity through remote sensing data can rely on the moving window technique, which divides remotely sensed imagery into user-defined squares (windows) to derive measures of heterogeneity. Examples are included in the rasterdiv R package (Rocchini et al., 2021). One of the most used <sup>130</sup> metrics included in the package is the Shannon entropy index H (Shannon, 1949):

$$H = -\sum_{i=1}^{N} p_i \ln p_i \tag{1}$$

where the relative abundance of every pixel reflectance value calculated as the ratio 131 between the actual value of the pixel  $i \in \{1, ..., N\}$  and the sum of the pixel values of 132 the moving window  $(p_i)$  in an image of N pixels is considered. It is usally calculated 133 of one layer images, such as a vegetation index or the first axis of a PCA. However, 134 Shannon's H does not consider the spectral distances among pixel reflectance values, 135 overestimating the heterogeneity of homogeneous surfaces (Rocchini et al., 2017). For 136 instance, when using Shannon's H, spectral values differing by a few decimals will 137 be treated the same as spectral values differing by several order of magnitudes. To 138 overcome this issue, Rao's Q index (Rao, 1982) can be used to include the pixel's 139 spectral distances in the calculation: 140

$$Q = \sum_{i=1}^{N} \sum_{j=1}^{N} d_{ij} \times p_i \times p_j$$
<sup>(2)</sup>

where  $d_{ij}$  is the spectral distance between pixel *i* and pixel *j* and  $p_i$  and  $p_j$  are the 141 relative abundances of the pixels i and j in an assemblage of N pixels. The spectral 142 distance between pixels  $d_{ij}$  can be calculated over any number of layers and using any 143 metric for the calculation of pairwise distances. For example, in the rasterdiv pack-144 age, the Rao function permits the calculation of Rao's Q chosing from "euclidean", 145 "manhattan", "canberra", "minkowski" and "mahalanobis" as the type of distance 146 calculated (Marcantonio et al., 2021). Both Shannon's H and Rao's Q are point de-147 scriptors of heterogeneity, showing only one part of its potential spectrum. Therefore, 148 the use of generalized entropies, where one single formula represents a parameter-149 ized version of an index, provides a continuum of heterogeneity metrics reflecting all 150 the characteristics of the heterogeneity spectrum. Rocchini et al. (2021) presented a 151 parametric version of Rao's Q allowing the characterisation of the dimensionality of 152

<sup>153</sup> heterogeneity in different ecosystems:

$$Q_{\alpha} = \left(\sum_{i,j=1}^{N} \omega_{ij} d_{ij}^{\alpha}\right)^{\frac{1}{\alpha}} \tag{3}$$

where  $d_{ij}$  is the spectral distance between pixel i and pixel j and  $\omega_{ij}$  is the combined 154 probability  $(1/N^2)$  of extracting pixels *i* and *j* in this order in an image of N pixels. 155 In other words, parametric Rao's Q is a generalized mean that measures the expected 156 distance between two randomly chosen pixels regulated by the parameter  $\alpha$ . The  $\alpha$ 157 parameter provides a continuum of potential diversity indices by regulating the weight 158 of  $d_{ij}$  with the highest values obtaining different types of means as it is increasing 159  $([\alpha \to 0] \Rightarrow \text{geometric}, \, [\alpha = 1] \Rightarrow \text{arithmetic}, \, [\alpha = 2] \Rightarrow \text{quadratic}, \, [\alpha = 3] \Rightarrow \text{cubic},$ 160 and so on till  $[\alpha \to \infty] \Rightarrow max_d)$ . 161

In this paper, we propose to calculate the area under the curve (AUC) constructed by applying the index parametric Rao's Q over a sequence of  $\alpha$  values. We want to verify if AUC can be used to quantify the width of the diversity spectrum calculated with parametric Q for each pixel, resulting in an image that can be exploited to monitor the change in the heterogeneity spectrum over time for a selected area.

### <sup>167</sup> 2.2 The R function

The function rasterdiv::accRao() exploits the function rasterdiv::paRao() to define the values of the parametric Rao's Q using a vector of alphas decided by the user. Accordingly, the values of parametric Rao's Q are calculated building a moving window around every pixel of the remote sensing image for every alpha selected. Then, the integral of the curve formed by the values of the parametric Rao's Q index obtained for every pixel is calculated.

## 174 **3** Examples

<sup>175</sup> In this section, we present one theoretical examples and two case studies for the new R <sup>176</sup> function proposed (accRao()). Specifically, AUC was calculated for one layer, multiand hyperspectral satellite images of areas afflicted by a sudden event that changed the
spatio-ecological heterogeneity of the area. We choose two images per case study of two
different moments in time and calculated the difference between the two, highlighting
the increase in heterogeneity.

#### <sup>181</sup> 3.1 A theoretical example

In this section, we will show how to use the function accRao() from the rasterdiv 182 package to calculate the accumulation function (integral) of Rao values obtained using 183 a range of alpha-values. We used a raster for the global average NDVI rescaled at 8-bit 184 available from rasterdiv. This raster was first cropped on the islands of Sardinia and 185 Corsica. In order to simulate the effects of an ecological perturbation, for example 186 widespread drought, we created a new raster with perturbed NDVI values for these 187 two islands. Pixels with NDVI higher than 150 were decreased using values from a 188 normal distribution centered on 50 with a standard deviation of 5. Then, we applied 189 accRao() both on the original and simulated raster by using alphas ranging from 1 to 190 10: 191

```
RaoAUC.before \leftarrow accRao(
   alphas = 1:10, #range of alphas
   x = ndvi.before, #raster layer
   dist_m = "euclidean", #method for the
                          #calculation of the
                          #spectral distance
   window = 3, #dimension of the moving window
   method = "classic", #specifies if the function
                        #is applied on a single
                        #layer or on a
                        #multidimensional system
   rasterAUC = TRUE, #specifies if the output
                      #will be a raster layer or
                      #a matrix
   na.tolerance = 0.4, #proportion of NA values
                        #tolerated
   np = 1 #number of cores which will be spawned
)
\texttt{RaoAUC.after} \leftarrow \texttt{accRao(alphas=1:10, x=ndvi.after,}
   dist_m="euclidean", window=3, method="classic",
   rasterAUC=TRUE, na.tolerance=0.4, np=1)
```

Afterwards, the difference between the two rasters, before and after the simulated perturbation, was calculated (Figure 1). Also, the average parametric Rao of the images in Figure 1 was calculated for every  $\alpha$  value, and the resulting curves are showed in Figure 2.

accRao() function derives the value of parametric Rao for each pixel using a moving
window algorithm. To illustrate how this methodology works, we applied paRao() on
a single group of neighbor pixels, which represents a moving window, from the two
NDVI rasters and with alphas ranging from 1 to 10 as follows:

```
#Selection of the 3x3 window
ndvi.pix.b \leftarrow ndvi.before[41:43, 21:23, drop=FALSE]
ndvi.pix.a \leftarrow ndvi.after[41:43, 21:23, drop=FALSE]
#Set the alpha interval
alphas = 1:10
#Set the number of pixels in the selected window
N = 3^2
#Function to calculate paRao over the set alphas
RaoFx \leftarrow function(alpha,N,D) {
  ( sum((1/(N^4)) * D^alpha )*2)^(1/alpha)
}
#Calculation of paRao before
RaoFx(alpha=a, N=N,D=as.vector(ndvi.pix.b))})
#Calculation of paRao after
rao.a \leftarrow sapply(alphas, function(a) {
  RaoFx(alpha=a, N=N, D=as.vector(ndvi.pix.a))})
```

From the values obtained (a parametric value for each alpha), the area under the curve was calculated integrating the results (Figure 3):

```
#Calculation of AUC before
RaoAUC.bf ← approxfun(x = alphas, y = rao.b)
RaoAUC.b ← integrate(RaoAUC.bf, lower = 1,
    upper = 10, subdivisions = 500)
#Calculation of AUC after
RaoAUC.af ← approxfun(x = alphas, y = rao.a)
RaoAUC.a ← integrate(RaoAUC.af, lower = 1,
    upper = 10, subdivisions = 500)
```

#### 205 3.2 Empirical examples

In this section, the accRao() function is tested on two real-world case studies by comparing remotely sensed images before and after a perturbation event. AUC is calculated on multi- and hyperspectral images, exploiting the information that every band holds to estimate the spatio-ecological heterogeneity.

#### 210 3.2.1 Example 1: Fire spread in the Kangaroo island (Australia)

This section focuses on the major fire-affected area of Kangaroo Island in January 2020, in particular on Flinders Chase NP and the associated Ravine Des Casoars Wilderness Protection Area. Two cloudless images from Copernicus Sentinel-2 (https: //scihub.copernicus.eu/) with a spatial resolution of 10m before (January 2019) and after (January 2021) were compared (Figure 4). The accRao() function was applied on the 2 multispectral images (Red, Green, Blue and NIR bands) using a moving window of 9×9 pixels and the parameter alpha was set to a range of 1 to 5:

```
#accRao() function
accRao(alphas = 1:5, x = kanga_multi,
    dist_m = "euclidean", window = 9,
    method = "multidimension", rasterAUC = TRUE,
    na.tolerance = 0.9, np = 1)
```

Subsequently, the difference between the obtained AUC images was calculated, with positive values meaning an increase in spatio-ecological heterogeneity (Figure 4). In this case, the AUC of Rao's Q profiles succeeded to highlight areas where the perturbation (fire) event caused an increase of spatial heterogeneity of vegetation which was more homogeneous (continuous woodland cover) before the perturbation.

#### 224 3.2.2 Example 2: Post fire in Santa Barbara, California

For the last empirical examples two hyperspectral images of a postfire scene in Santa Barbara (California) were downloaded from AVIRIS https://aviris.jpl.nasa.gov/ platform. The first image is from June 2009, the second from June 2011 in order to visualize the recovery of the vegetation after the fire event (see Figure 5). The accRao() function was applied over all the 224 bands of the two images using a moving window of  $9 \times 9$  pixels and setting the  $\alpha$  parameter to a range of one to 5:

```
#accRao() function
accRao(alphas = 1:5, x = santabarbara_hyper,
    dist_m = "euclidean", window = 9,
    method = "multidimension", rasterAUC = TRUE,
    na.tolerance = 0.9, np = 1)
```

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Subsequently, the difference between the obtained AUC images was calculated as in

the previous examples (Figure 6). The difference between the obtained AUC highlights
subtle changes of spatio-ecolocical heterogeneity in the studied area between 2009 and
2011.

## 236 4 Discussion

The study of landscape structure has been steadily growing in recent years (e.g., 237 Lichstein et al., 2002; Saravia, 2015) with the development of several methodologies 238 and approaches, which have been tested ecosystems and supported in the scientific 239 literature (see Bar-Massada and Wood, 2014). In particular, the use and availability of 240 remote sensing data have made it possible to assess specific heterogeneity patterns over 241 various ecosystems, with increasing performance in terms of spectral/spatial/temporal 242 characteristics, opening up new possibilities for exploring complex ecological processes. 243 Using our algorithm, environmental heterogeneity is estimated by the range of 244 spectral values associated to the spatial variability within a given habitat. Hence, 245 environmental heterogeneity can be evaluated contiguously, from regional to conti-246 nental extents, according to the remote sensing data used and the spatial extent of 247 the analysis. Among the heterogeneity metrics, parametric Rao's Q adds a layer of 248 information to classical estimates of heterogeneity from remotely sensed multispectral 249 data. This index considers pairwise pixel spectral distance to separate areas with high 250 richness but low evenness from those with low richness but high evenness (Rocchini et 251 al., 2017). 252

In addition, the parametric Rao's Q can be calculated in a multivariate system such as a multi-temporal system, i.e. long time series, in order to improve the assessments and prediction of changes in spatio-ecological heterogeneity over space and time (Rugani and Rocchini, 2016). Also, by considering multiple bands, it has a higher capability to discern subtle diversity changes over the landscape (Torresani et al., 2019).

In this paper, all the potential facets of heterogeneity were investigated by parameterizing the Rao's Q metric and calculating the area under the curve of continuous entropy profiles. This would be particularly useful when dealing with multitemporal sets, with increases or decreases of heterogeneity provoked by different ecological processes like drought (subsection 3.1, see also Jiao et al., 2020) and fire (subsection 3.2.1, see also Chuvieco and Kasischke, 2007; subsection 3.2.2).

The application of AUC on Rao's Q in before / after ecological perturbation sce-265 narios can help pointing out areas with the highest difference in spectral heterogeneity, 266 by considering the whole heterogeneity continuum. For example, subsection 3.2.2 of 267 two postfire scenes shows the sensibility of the algorithm in highlight even subtle land-268 scape changes using multiple bands for the analysis. Heterogeneity of ecosystems is 269 multifaceted in its very nature. As stressed by (Gorelick, 2011) there is no "true het-270 erogeneity" measurement since important holistic aspects of ecosystems are inevitably 271 lost once making use of single metrics. From this point of view, the proposed general-272 ized entropy, based on a parameterization of the Rao's Q entropy (and its area under 273 the curve) can help catching the multidimensionality of ecosystem heterogeneity com-274 ponents (Nakamura et al., 2020), avoiding the intrinsic fallacy of a single best index 275 of true heterogeneity (Gorelick, 2011). 276

Moreover, the Rao's Q original formula directly takes into account the distance 277 among values (pixel reflectances once applied to remote sensing imagery). This leads to 278 the possibility of accounting for the turnover among reflectances, also known as beta-279 diversity in ecology (Rocchini et al., 2018). Since little consensus has been reached as 280 to general measures of heterogeneity / beta-diversity measurement in literature (Koleff 281 et al., 2003), the aforementioned use of a generalized metric like the parametric Rao's 282 Q helps detecting gradients in reflectance beta-diversity change (turnover) over space, 283 otherwise hidden when relying on point descriptors of heterogeneity, i.e. single metrics 284 like the commonly used Shannon and Simpson indices in remote sensing applications 285 (Nagendra, 2002). In other words, while a wide range of approaches has been used to 286 catch the variation of ecosystem properties, finding ways to generalize heterogeneity 287 measurement could represent a consistent approach to describe heterogeneity patterns 288 change in space and time (Haralick & Kelly, 1969). 289

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The use of a continuum of diversities as in the parametric Rao's Q leads to the

understanding of hidden parts of the whole diversity of dimensionalities (Nakamura 291 et al., 2020). Increasing alpha in Equation 3 will increase the weight of higher dis-292 tances among different values until reaching the maximum distance value possible 293 (Rocchini et al., 2021). For this reason, spatio-ecological heterogeneity values of the 294 parametric Rao's Q increase with each alpha progressively added to the calculation 295 constructing a curve for every moving window built around each pixel (Rocchini et 296 al., 2021). Consequently, applying an integral, it is possible to calculate the area un-297 der every pixel's window area curve obtaining a new spatio-ecological heterogeneity 298 metric, AUC. Hence, the accRao() function can highlight the differences before and 299 after an ecological perturbation both in the theoretical and in the empirical examples 300 (Figures 1, 4 and 6) showing the change in the whole heterogeneity continuum and 301 being able to detect both: (i) spatially wide heterogeneity change patterns, as in the 302 Kangaroo Island's fires example (see subsection 3.2.1), as well as (ii) spatially local-303 ized differences in space and time, as in the post fire in Santa Barbara example (see 304 subsection 3.2.2). 305

The three examples proposed in section 3, show the application of AUC on one 306 layer (subsection 3.1), multispectral (subsection 3.2.1) and hyperspectral 3.2.2 satellite 307 images. However, for the hyperspectral images it is difficult to address a cause for the 308 heterogeneity change: because of the high number of bands exploited for the analysis 309 we can't know which ones weight more in the measure of the index. Analysis like the 310 Principal Component Analysis (PCA) or correlation matrices can help to highlight 311 the bands which give more contribution in the calculation of the spatio-ecological 312 heterogeneity. 313

Also, in the empirical case studies only a range of alpha between 1 and 5 was tested because of the high computational complexity of the function accRao() as it is now. We are actually working to speed up the algorithm, so it would be interesting in a future study to test different ranges of alpha. In this context, it would also be helpful the study of the influence of the number of bands and their resolution on the measure of AUC, as highlighted by the Santa Barbara subsection (see subsection 3.2.2).

<sup>320</sup> In conclusion, the integration over an alpha range is more convenient than having

to choose a single alpha level as the most representative level of diversity. This task is often complicated as there is no direct interpretation for the meaning of indexes calculated with different alphas. Here, we propose the way forward to re-conciliate the advantage of having a single metrics without the need of choosing a single alpha value.

## 326 5 Conclusion

In this paper, we provided a practical demonstration of the effectiveness of a method 327 that can supply meauseres of generalized entropy at different spatial scales and in 328 different contexts. Generalized means represent an effective tool to develop a uni-320 fying notation for a large family of parametric diversity and dissimilarity functions 330 (Ricotta et al., 2021). Indeed, binding different heterogeneity metrics in order to 331 analyze ecosystem changes proved to be a reliable approach to enhance the output 332 information. Although remote sensing data have long held the promise of transform-333 ing environmental monitoring efforts, publicly accessible tools leveraging these data 334 to achieve actionable in-sights have been lacking. We suggest that Rao's AUC can 335 be useful to identify areas more vulnerable to environmental changes, and to develop 336 and implement appropriate habitat management plans and environmental policies. 337

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The rasterdiv package that contains the new function proposed can be downloaded at https://github.com/mattmar/rasterdiv or directly from the CRAN (https:// 347 CRAN.R-project.org/package=rasterdiv). The hyperspectral images of Santa Bar-

bara of June 2009 and 2011 can be respectively retrieved from https://popo.jpl.

nasa.gov/avcl/y09\_data/f090826t01p00r08.tar.gz and https://popo.jpl.nasa.

350 gov/avcl/y11\_data/f110719t01p00r19.tar.gz. The images of Kangaroo Island can

<sup>351</sup> be retrieved from https://scihub.copernicus.eu/dhus/#/home.

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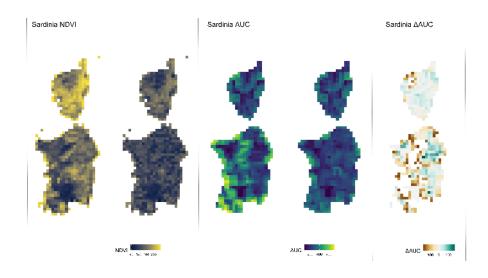


Figure 1: From left to right: the NDVI images of Sardinia and Corsica before and after the simulated perturbation, the correspondent AUC images and their difference after - before the simulated perturbation.

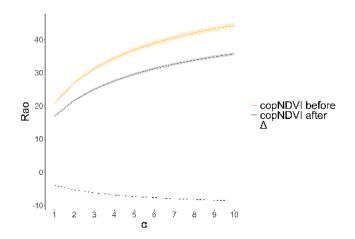


Figure 2: Three curves representing respectively: the mean values of parametric Rao's Q (i) before (yellow) and (ii) after (grey) the simulated ecological perturbation (drought) of Figure 1, their correspondent confidence intervals and (iii) their difference (after - before, dashed line) over increasing alphas.

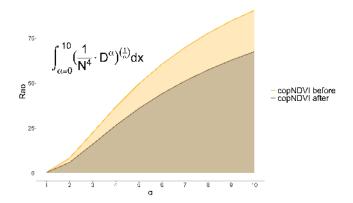


Figure 3: Curves representing the values of parametric Rao's Q for one pixel before (yellow) and after (grey) the simulated ecological perturbation (drought) of Figure 1 over increasing alphas. The area under the curve (AUC) is highlighted.

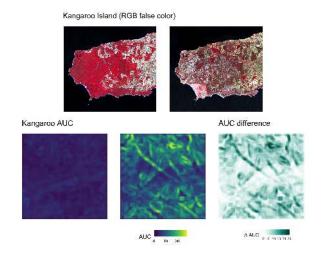


Figure 4: On top left, the Kangaroo Island before and after the fires (the area used for the analysis is highlighted) and the selected area before and after the fire in RGB false color (NIR, red, green); on the right the correspondent AUC images and their difference after - before the fire.

# Santa Barbara RGB



Figure 5: Post fire in Santa Barbara 2009 (left) and 2011 (right). The area within the square is the studied area.

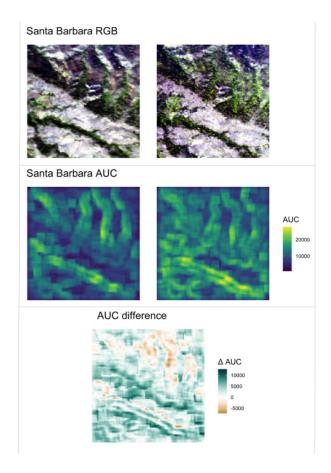


Figure 6: From the top: RGB images of the study area (Santa Barbara, CA) in 2009 and 2011, the correspondent AUC images and their difference 2011 - 2009.